

Question 1. [5 points] State a big-O upper bound on the worst case running time of the given method, where the problem size N is the number of elements in the `list` parameter. You can assume that the call to `equals` is $O(1)$. Explain your answer briefly.

```
public static<E> int find(ArrayList<E> list, E elt) {  
    for (int i = 0; i < list.size(); i++) { —  $N$  times  
        if (list.get(i).equals(elt)) {  
            return i; }  
        }  
    }  
    return -1;  
}
```

is $O(1)$ for `ArrayList`

$N \cdot O(1)$ is $O(N)$

Question 2. [5 points] State a big-O upper bound on the worst case running time of the given method, where the problem size N is the number of elements in the `list` parameter. You can assume that the call to `equals` is $O(1)$. Explain your answer briefly.

```
public static<E> int find(LinkedList<E> list, E elt) {  
    for (int i = 0; i < list.size(); i++) { —  $N$  times  
        if (list.get(i).equals(elt)) {  
            return i; }  
        }  
    }  
    return -1;  
}
```

is $O(N)$ for `LinkedList`
(must skip $O(N)$ elements on average)

~~$N \cdot O(N)$~~ is $O(N^2)$

Question 3. [5 points] Complete the following generic method. It takes two values of type E, and a Comparator that can compare values of type E, and returns the smaller of the two values.

Hint: use the comparator's compare method to compare the two values.

```
public static<E> E min(E val1, E val2, Comparator<E> comp) {  
    if ( val1 comp.compare(val1, val2) < 0 ) {  
        return val1;  
    } else {  
        return val2;  
    }  
}
```

Question 4. [5 points] Indicate whether a stack, or a queue would be best for implementing each of the following:

- (a) A keyboard buffer: *queue*
- (b) A text editor "undo" operation: *stack*
- (c) Buffering events in a video game: *queue*
- (d) Capturing the most recent 30 seconds of security video: *queue*
- (e) Reversing the contents of a list: *stack*

Question 5. [5 points] For a certain card game, the value of each card in a Suit is multiplied by its Suit's multiplier factor (an integer). Using the given Suit enum, declare and create a Map that allows the user to retrieve a Suit's multiplier factor, where SPADES = 8X, HEARTS = 4X, DIAMONDS = 2X and CLUBS = 1X. Be sure to show how the map is populated.

```
public enum Suit {
    SPADES,
    HEARTS,
    DIAMONDS,
    CLUBS
}
Map<Suit, Integer> m = new HashMap<Suit, Integer>();
m.put(Suit.SPADES, 8);
m.put(Suit.HEART, 4);
m.put(Suit.DIAMONDS, 2);
m.put(Suit.CLUBS, 1);
```

Question 6. [5 points] Given the following two enums, declare and create a Map that cross-references a Suit with its Color. Be sure to show how the map is populated.

```
public enum Suit {
    SPADES,
    HEARTS,
    DIAMONDS,
    CLUBS
}

public enum SuitColor {
    RED,
    BLACK
}

Map m = new HashMap<Suit, SuitColor>();
m.put(Suit.SPADES, SuitColor.BLACK);
m.put(Suit.HEARTS, SuitColor.RED);
m.put(Suit.DIAMONDS, SuitColor.RED);
m.put(Suit.CLUBS, SuitColor.BLACK);
```

Question 7. [10 points] Consider the following method to compute an iteration count to test whether a complex number is in the Mandelbrot set:

```
public int computeIterCount(Complex c){
    Complex z = new Complex(0, 0);
    int count = 0;

    while (z.getMagnitude() < 2 && count < MAX_COUNT){
        z = z.multiply(z).add(c);
        count++;
    }
    return count;
}
```

(a) Implement a recursive version of this computation:

```
// Recursive version
public int computeRecursiveIterCount(Complex c, Complex z, int count){
    if (count >= MAX_COUNT || z.getMagnitude() >= 2.0) {
        return count;
    }

    return computeRecursiveIterCount(c, z.multiply(z).add(c),
        count + 1);
}
```

Make sure you check a base case or base cases, that the recursive call(s) work towards a base case, and that the result of the recursive call or calls is extended to be a solution for the overall problem.

(b) Is it a good idea to implement this computation recursively? Briefly explain why or why not.

No, because very deep recursions can throw Stack Overflow Error.

Question 8. [5 points] Consider the following methods, which attempt to compute the n 'th member of the Fibonacci sequence using memoization:

```
public static int fib(int n) {  
    return fibMemo(n, new int[n+1]);  
}  
  
private static int fibMemo(int n, int[] memo) {  
    if (n == 0 || n == 1) {  
        return 1;  
    } else {  
        if (memo[n] == 0) {  
            memo[n] = fib(n-2) + fib(n-1);  
        }  
        return memo[n];  
    }  
}
```

should call fibMemo

Briefly explain the error in this code, and how to fix it.

Calling fib rather than fibMemo creates a new (empty) memoization table. So, answers to previously encountered subproblems are not saved.

Solution is to change the recursive calls to

$$\text{fibMemo}(n-2, \text{memo}) + \text{fibMemo}(n-1, \text{memo})$$

Question 9. [10 points] Given the constructor for the CalculateTask (which implements Runnable)

```
public CalculateTask(int[] arr, int start, int end)
```

where start and end specify the portion of array arr to process for each thread, complete the following fork/join code to process the array in parallel, using numThreads threads.

Hint: think about how you can divide up the elements of the array to split the work equally between tasks.

```
int chunk = arr.length / numThreads;
```

```
Thread[] threads = new Thread[numThreads];
```

```
CalculateTask[] tasks = new CalculateTask[numThreads];
```

```
// create CalculateTasks and specify range to be processed
```

```
for (int i = 0; i < numThreads; i++) {
```

```
    tasks[i] = new CalculateTask(arr,  
        i * chunk, (i + 1) * chunk);
```

```
}
```

```
// create Threads, initialize from tasks array,
```

```
// and start the threads
```

```
for (int i = 0; i < numThreads; i++) {
```

```
    threads[i] = new Thread(tasks[i]);  
    threads[i].start();
```

```
}
```

```
// wait for the threads to complete
```

```
try {
```

```
    for (int i = 0; i < numThreads; i++) {
```

```
        threads[i].join();
```

```
    }
```

```
} catch (InterruptedException e) {
```

```
    System.out.println("Error waiting for thread to complete: " + e);
```

```
}
```